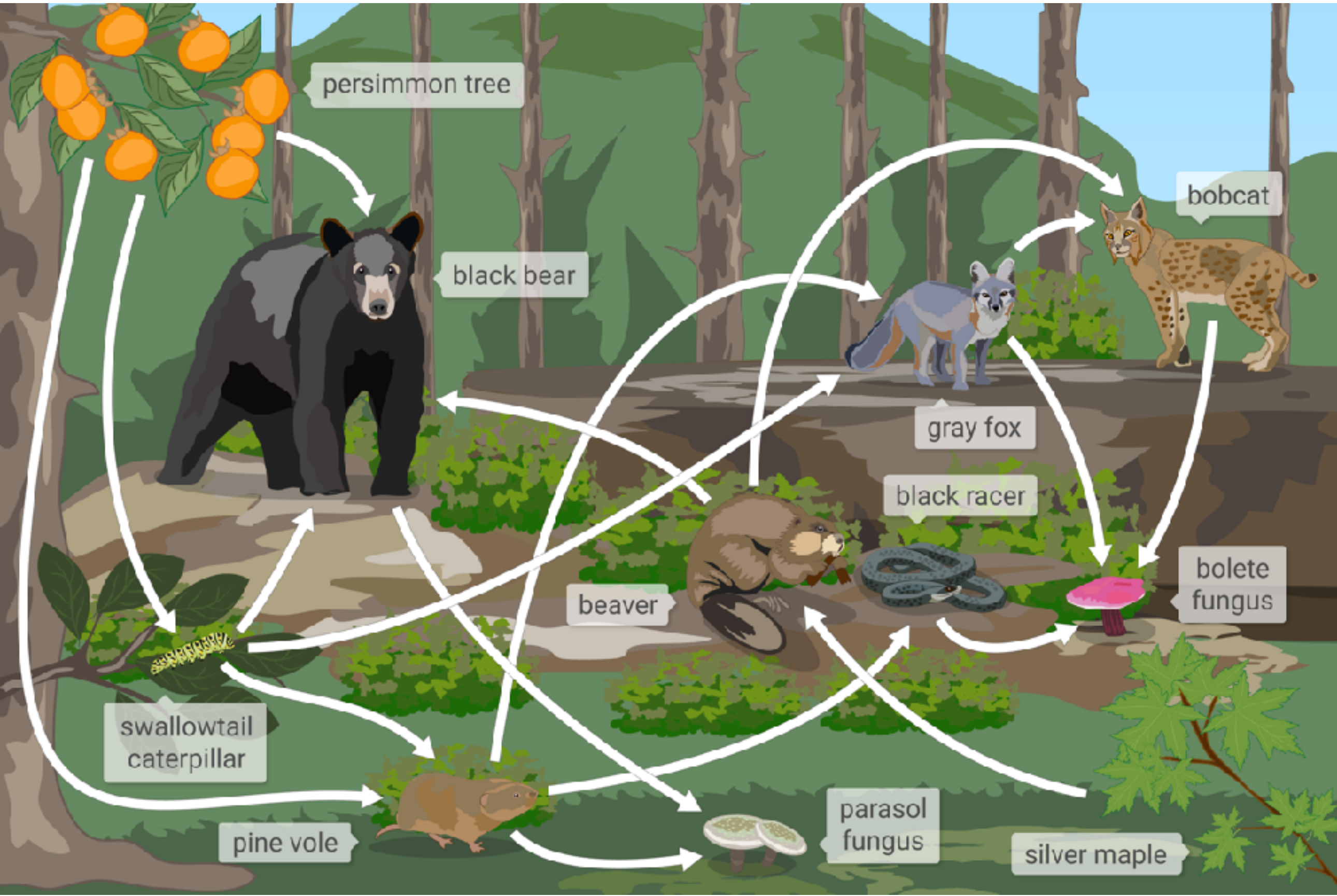
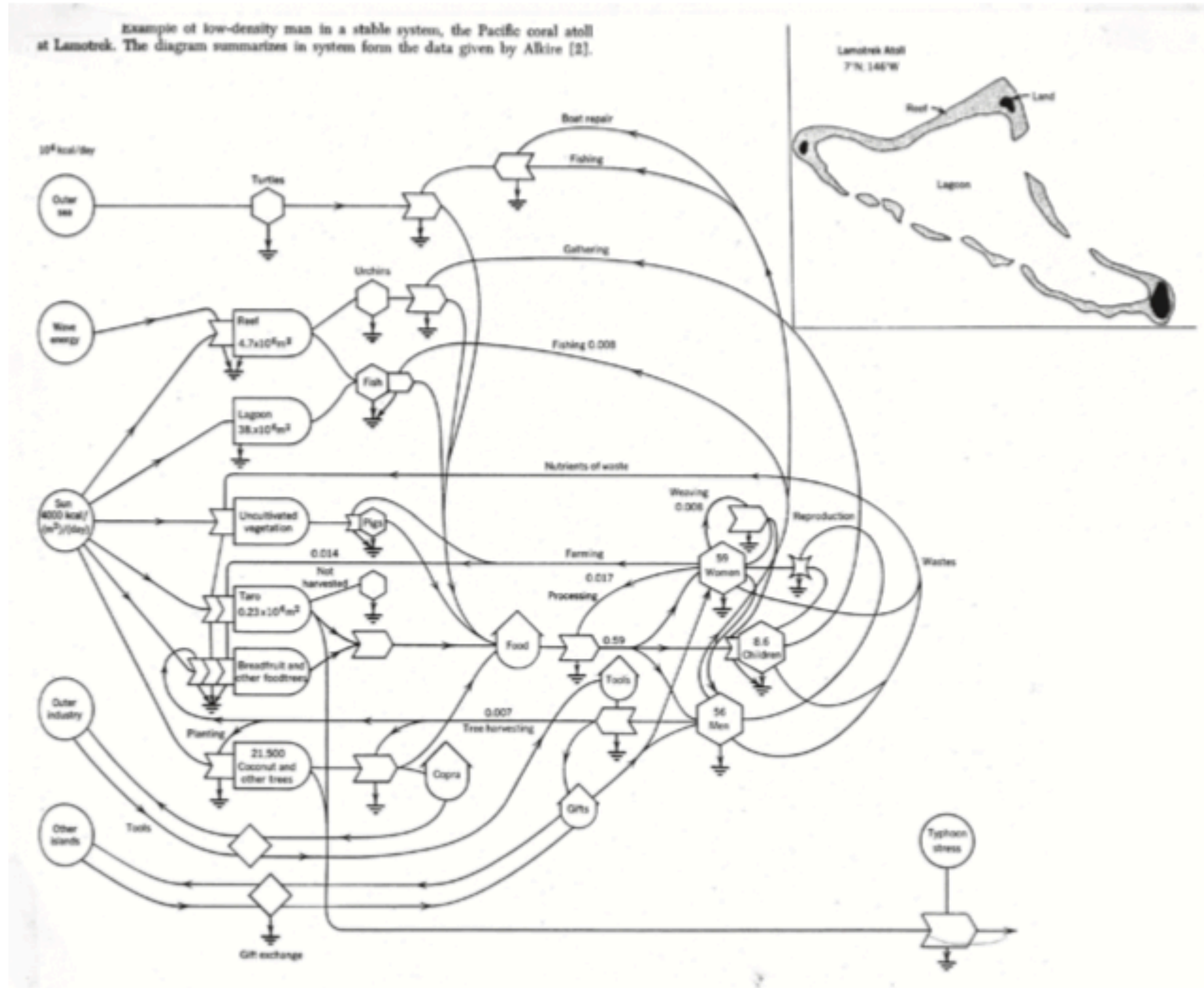
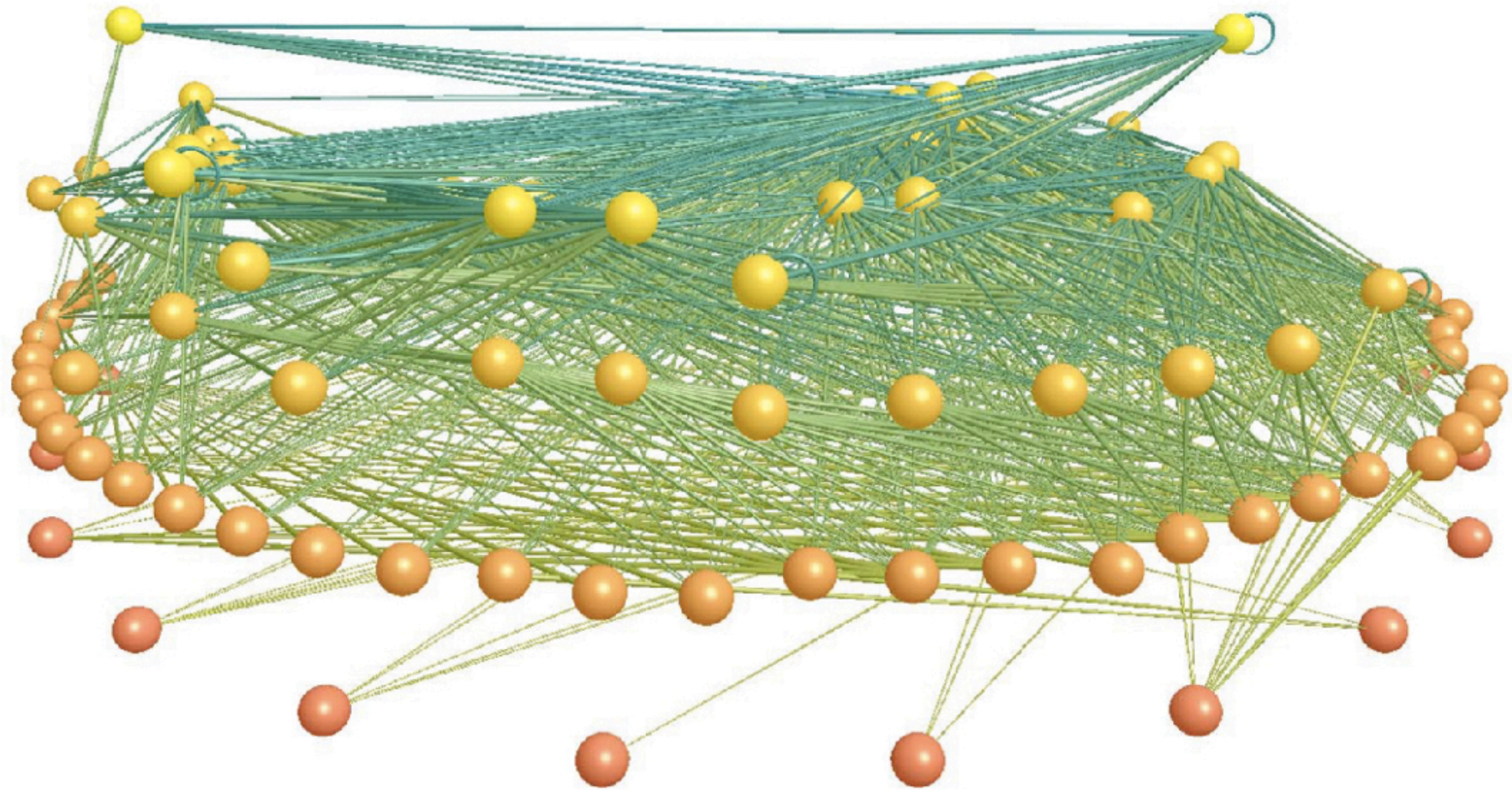


food webs



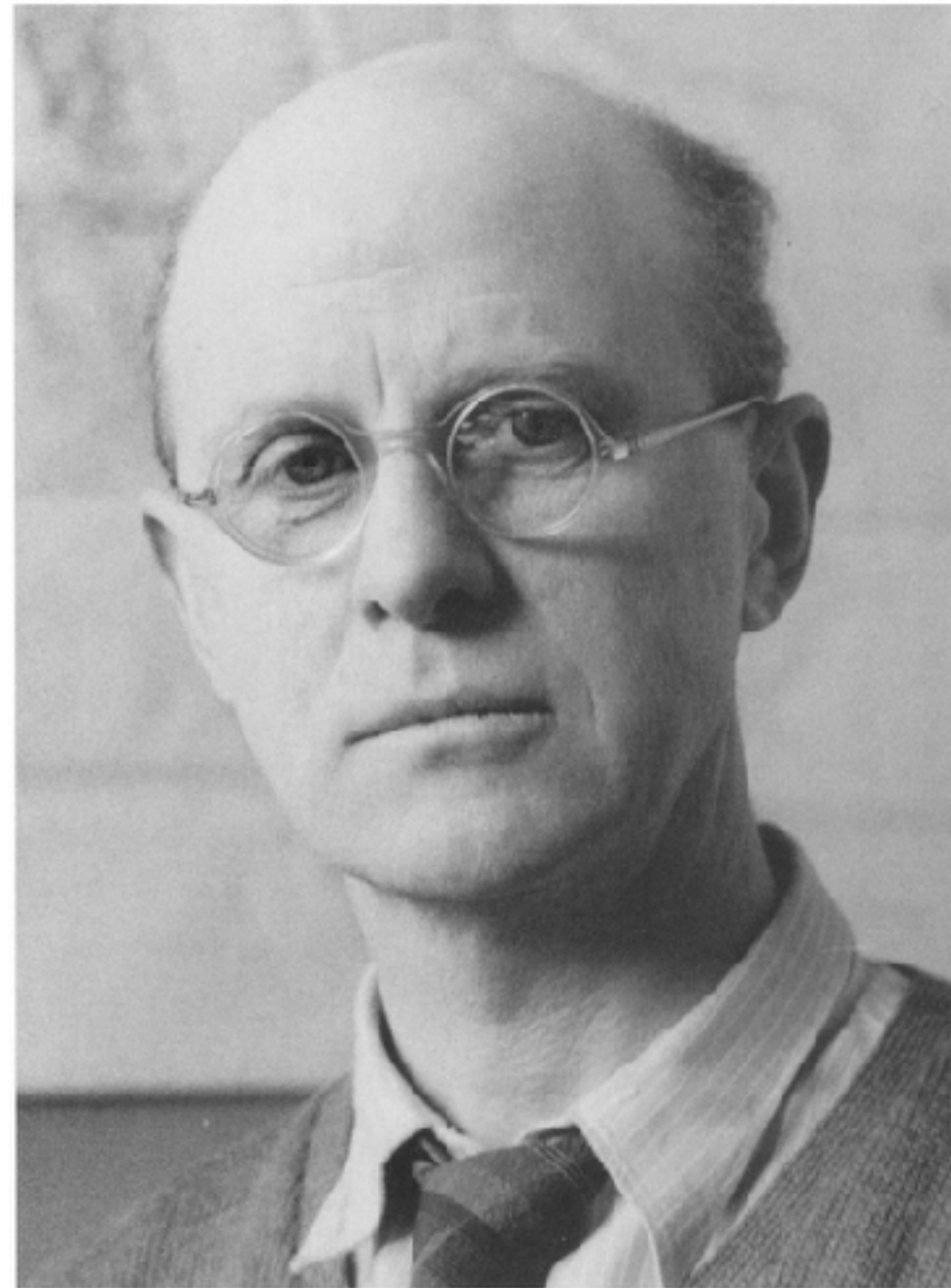


Howard T. Odum 1971



Food webs as complex networks (Dunne, Martinez, and Williams)

stability and complexity (I)



Charles Elton

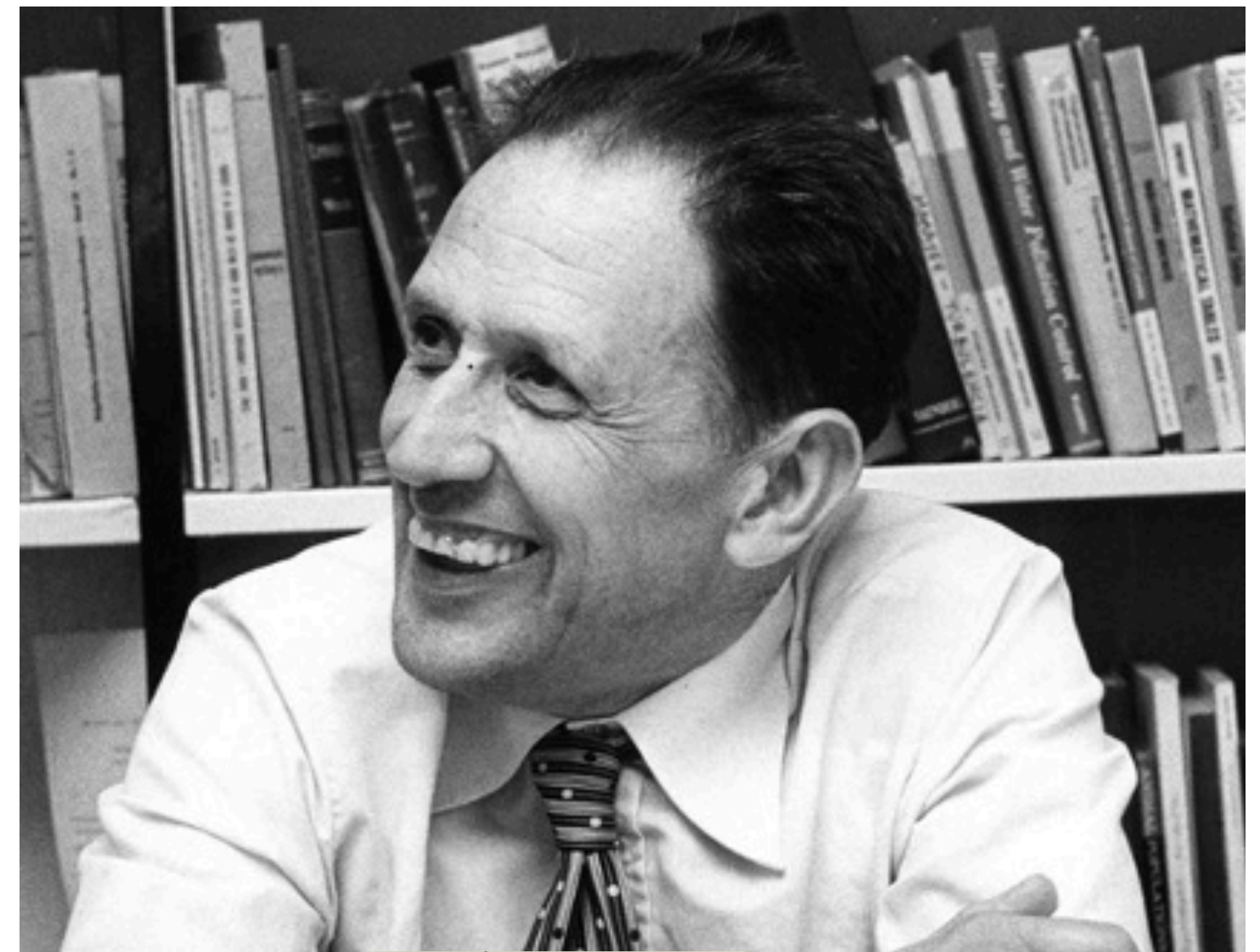


Robert MacArthur



Eugene P. Odum

Photo by Gittings



Ramón Margalef

stability and complexity (I)



Robert MacArthur

FLUCTUATIONS OF ANIMAL POPULATIONS, AND A MEASURE OF COMMUNITY STABILITY¹

July, 1955

NOTES AND COMMENT

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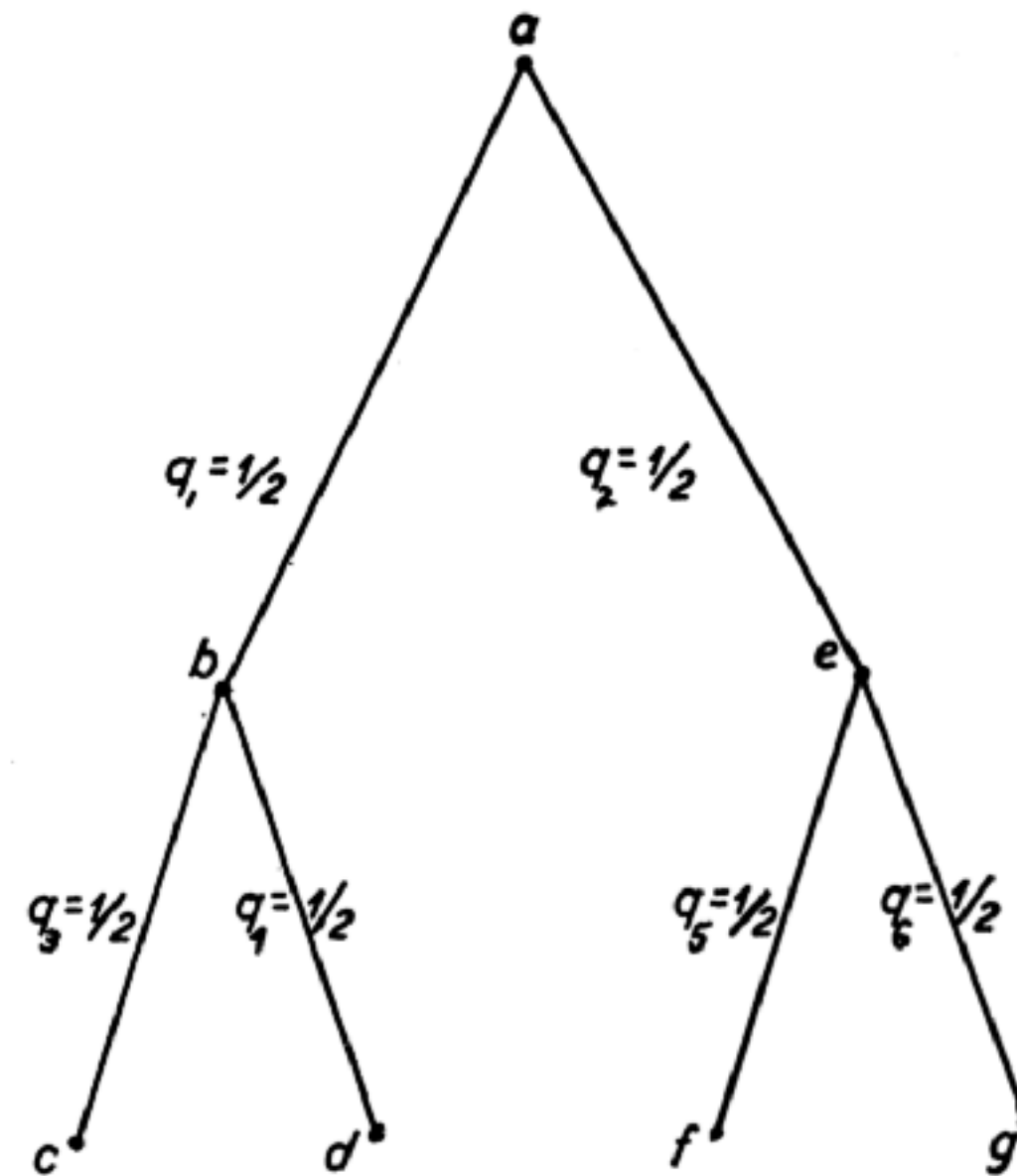


FIG. 3. A food web. *a*, *b*, *c*, *d*, *e*, *f* and *g* are species, and q on the line joining predator and prey signifies that fraction of the total number of prey species formed by the prey species in consideration.

$$S = - \sum p_i \log p_i = -4 \left(\frac{1}{4} \log \frac{1}{4} \right) = \log 4$$

“Suppose, for some reason, that one species has an abnormal abundance... The less effect this abnormal abundance has on the other species, the more stable the community.”

“The amount of choice which the energy has in following the paths up through the food web is a measure of the stability of the community.”

“If each species has just one predator and one prey the stability should be minimum, ... as the number of links in the food web increases the stability should increase.”

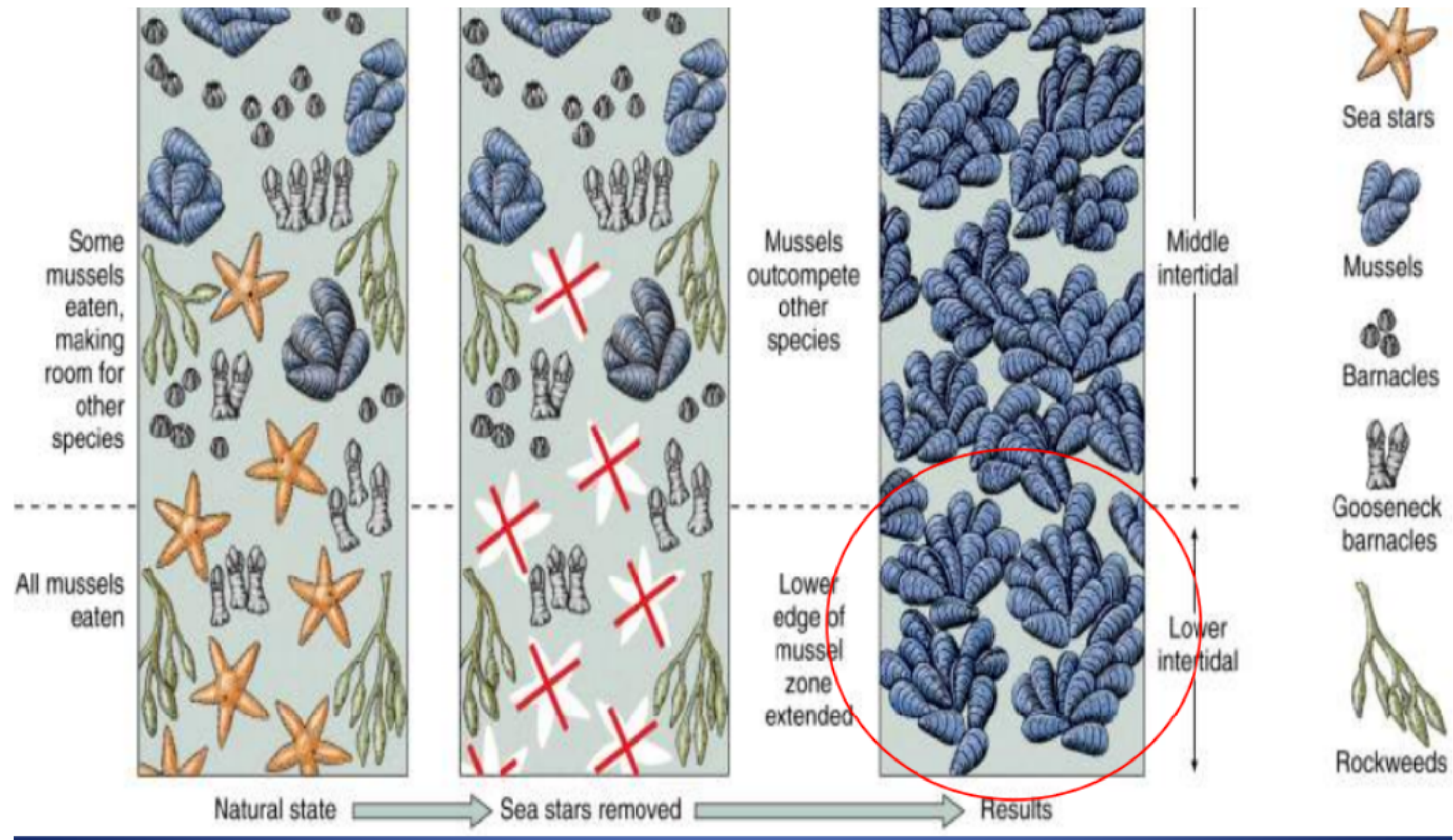
trophic cascades



FOOD WEB COMPLEXITY AND SPECIES DIVERSITY

ROBERT T. PAINE

Department of Zoology, University of Washington, Seattle, Washington



stability and complexity (II)

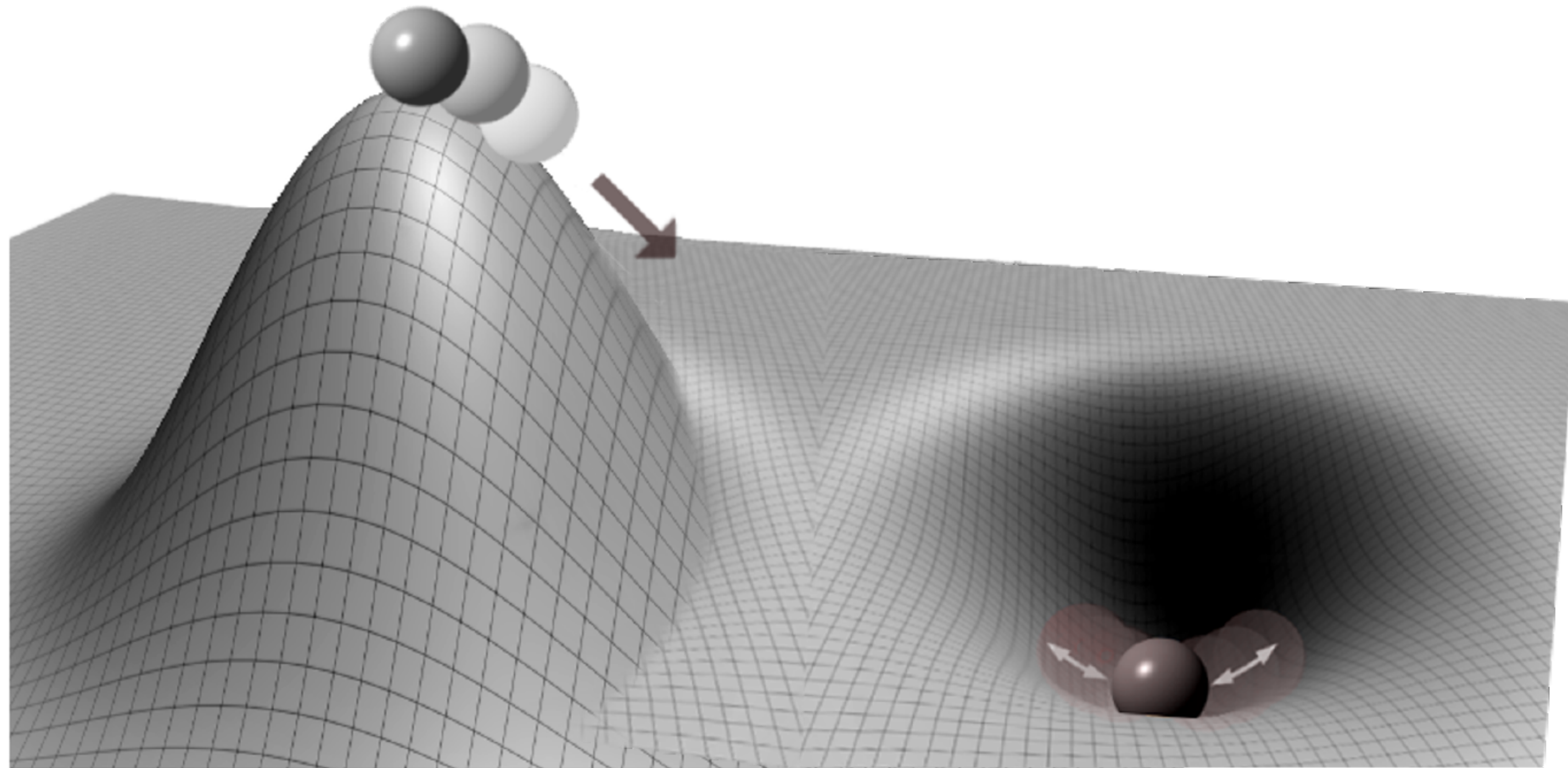


Will a Large Complex System be Stable?

Gardner and Ashby¹ have suggested that large complex systems which are assembled (connected) at random may be expected to be stable up to a certain critical level of connectance, and then, as this increases, to suddenly become unstable. Their conclusions were based on the trend of computer studies of systems with 4, 7 and 10 variables.

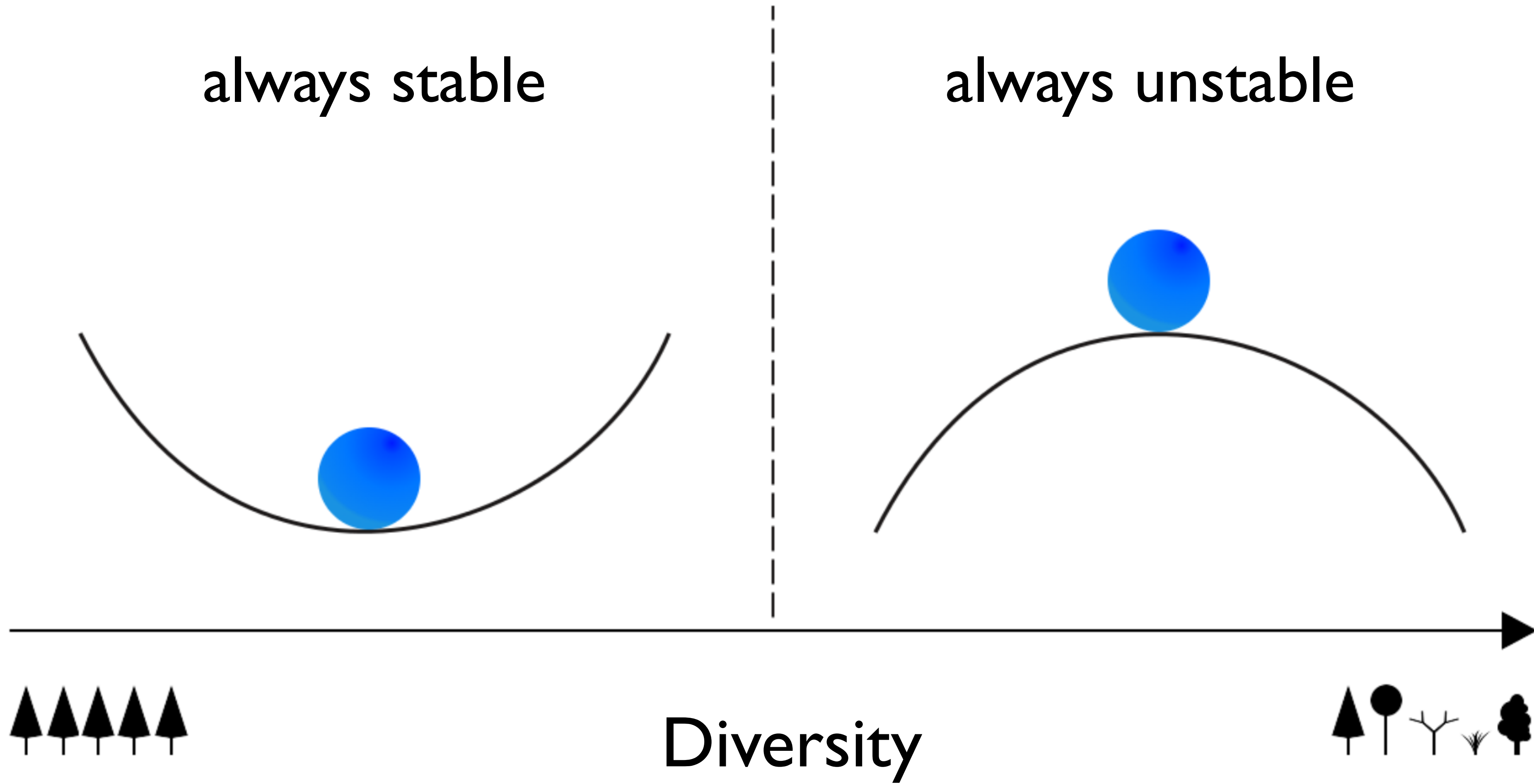
Here I complement Gardner and Ashby's work with an analytical investigation of such systems in the limit when the number of variables is large. The sharp transition from stability to instability which was the essential feature of their paper is confirmed, and I go further to see how this critical transition point scales with the number of variables n in the system, and with the average connectance C and interaction magnitude α between the various variables. The object is to clarify the relation between stability and complexity in ecological systems with many interacting species, and some conclusions bearing on this question are drawn from the model.

stability and complexity (II)



always stable

always unstable



stability and complexity (II)



a food web is stable if (May 1972):

interaction strength

number of species

$$\alpha < (n C)^{-\frac{1}{2}}$$

connectivity

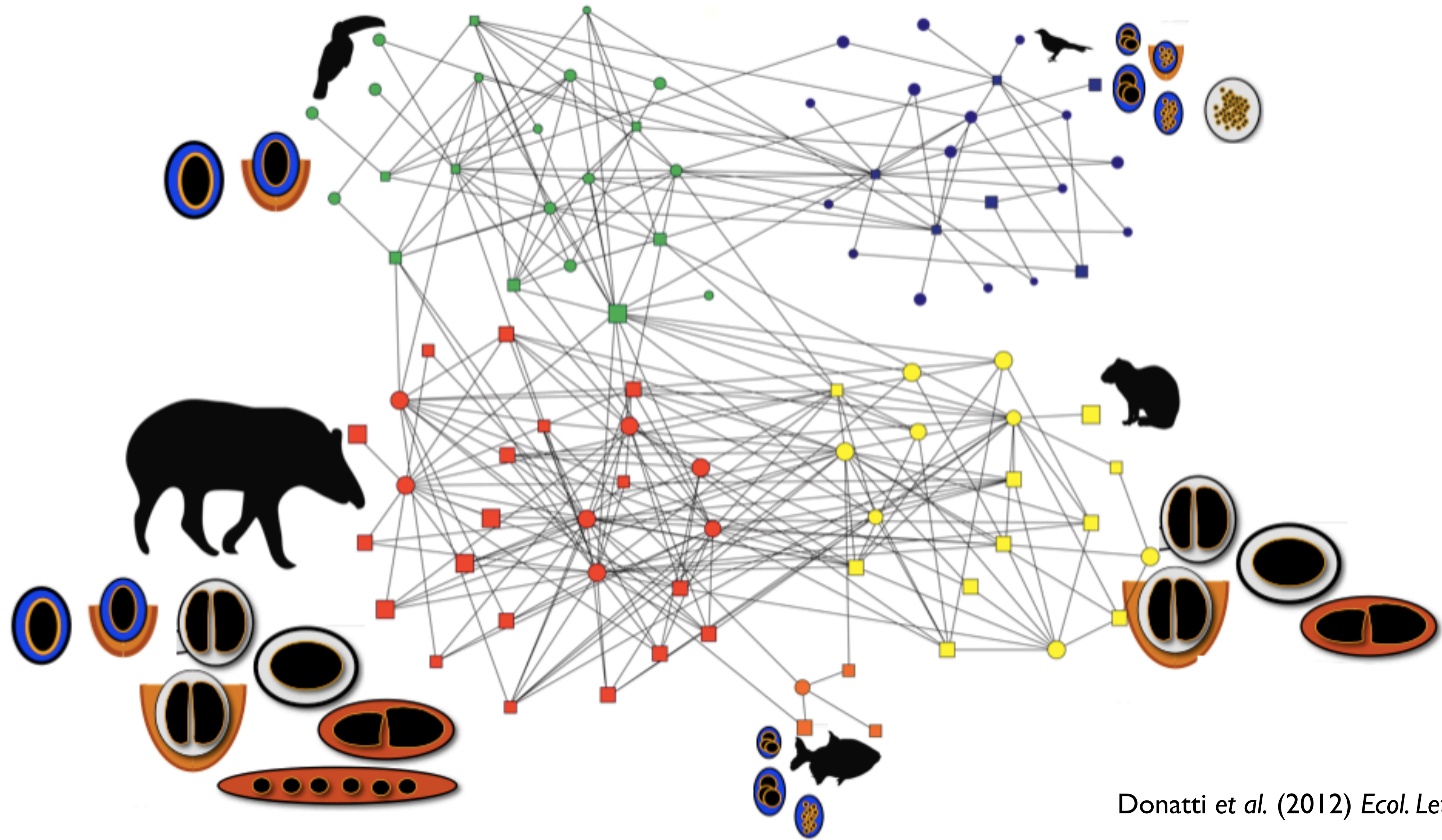
stability and complexity (II)



Will a Large Complex System be Stable?

Such examples suggest that our model multi-species communities, for given average interaction strength and web connectance, will do better if the interactions tend to be arranged in “blocks”—again a feature observed in many natural ecosystems.

May 1972, *Nature* 238: 413-414



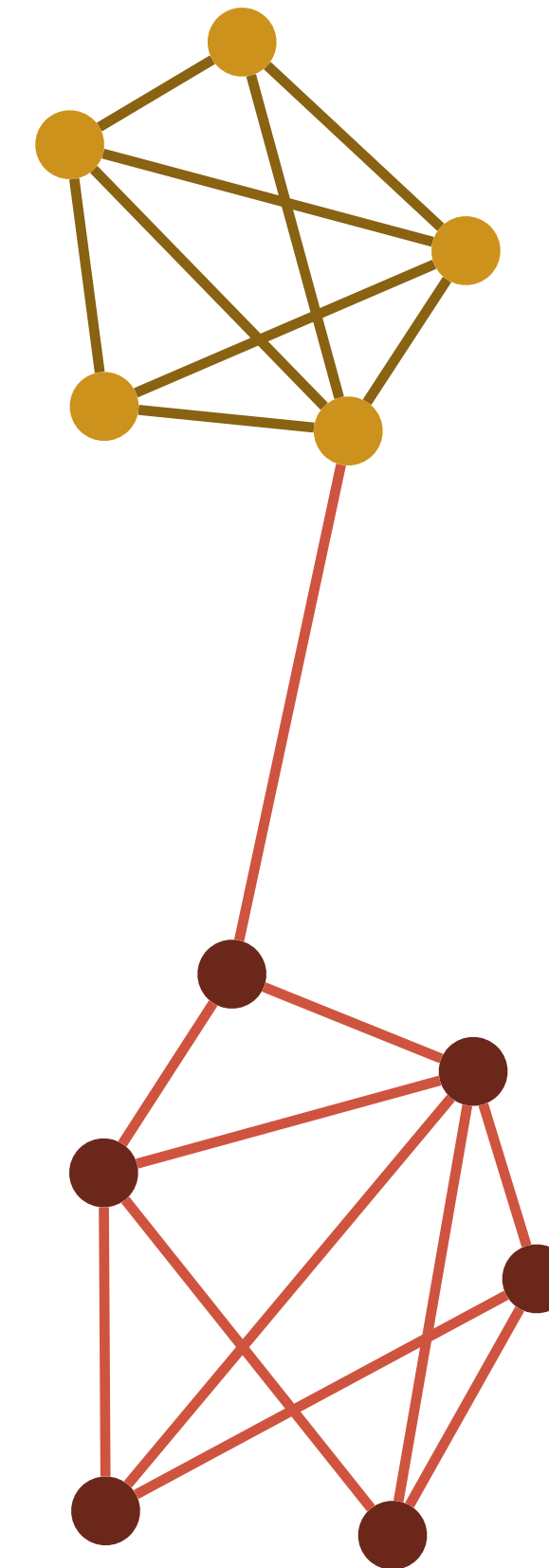
Donatti et al. (2012) *Ecol. Lett.*

modularity

$$M = \sum_{\text{all modules } s} \left[\frac{l_s}{L} - \left(\frac{d_s}{2L} \right)^2 \right]$$

fraction of interactions within module i

expected fraction of interactions within module i

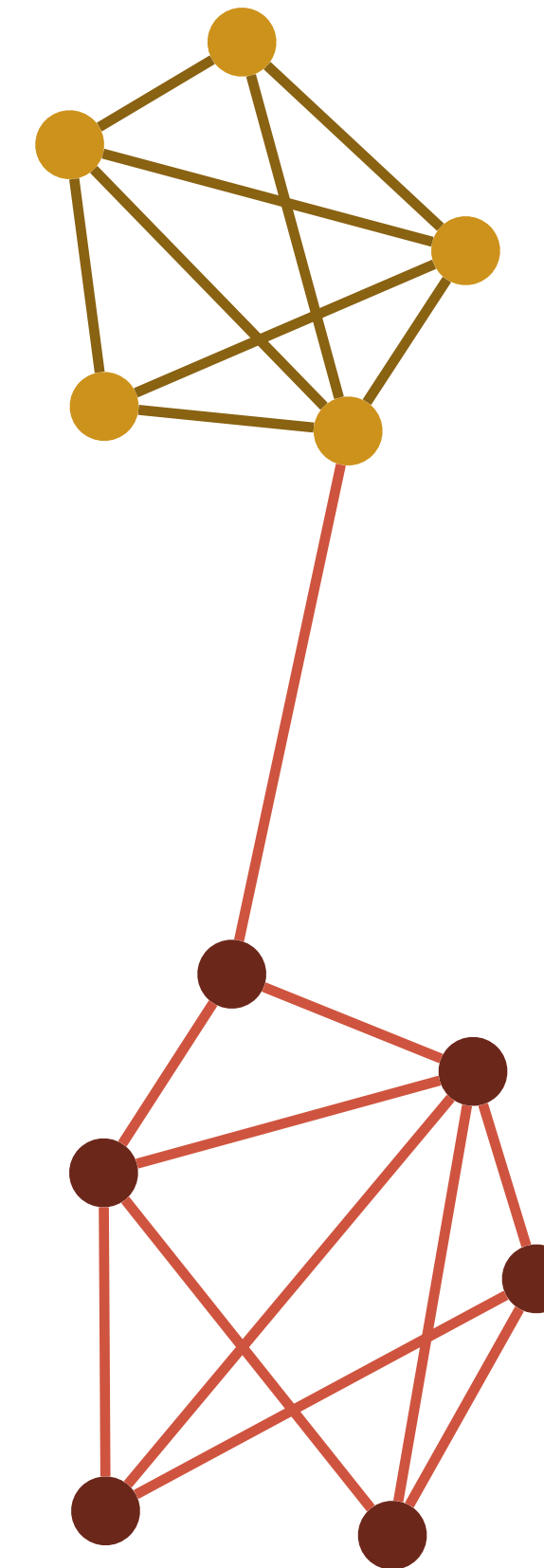


$$M = \sum_{\text{all modules } s} \left[\frac{l_s}{L} - \left(\frac{d_s}{2L} \right)^2 \right]$$

of interactions inside module s

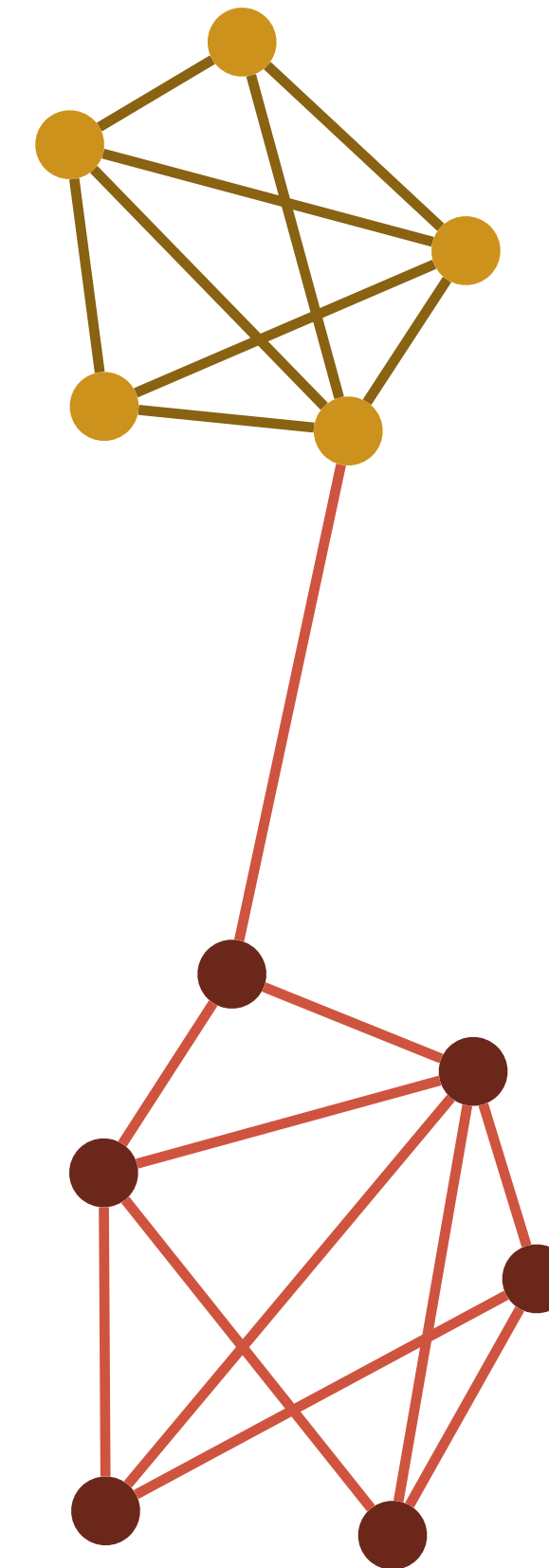
sum of the species' degree inside module s

of interactions in the whole network



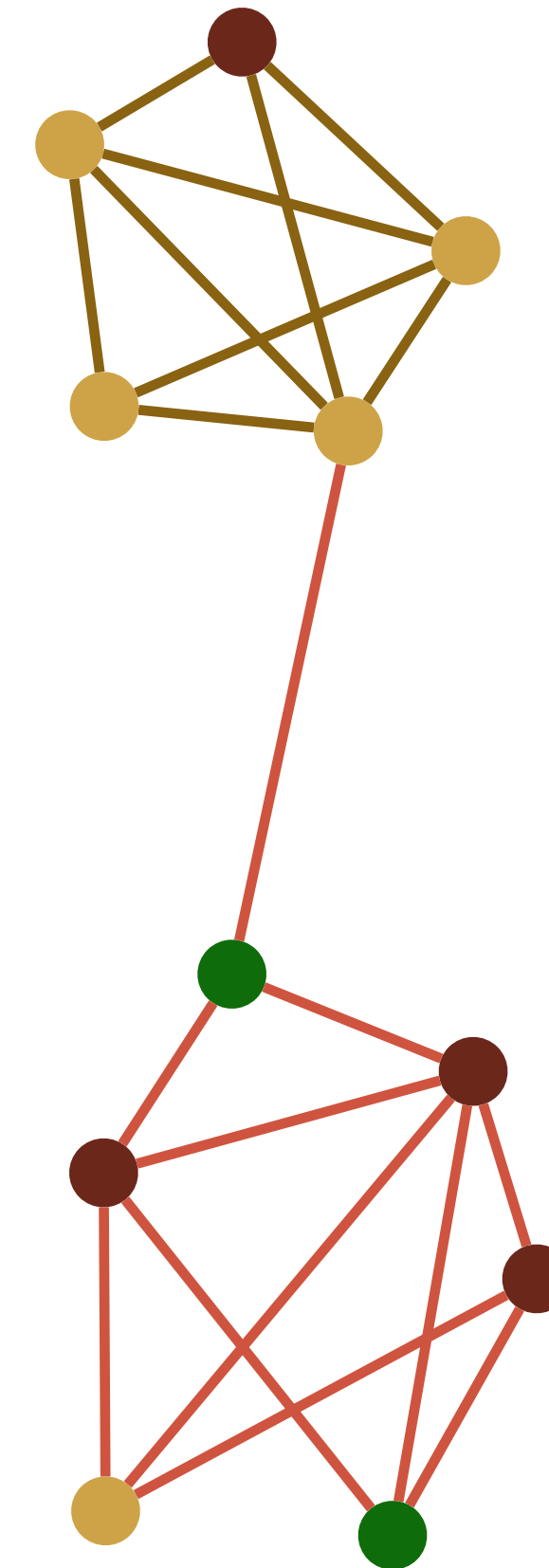
how to find the modules?

$$M = \sum_{\text{all modules } s} \left[\frac{l_s}{L} - \left(\frac{d_s}{2L} \right)^2 \right]$$



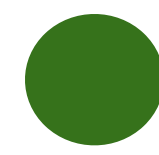
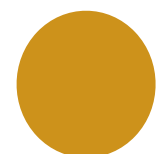
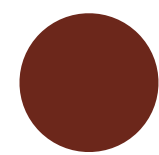
how to find the modules?

$$M = \sum_{\text{all modules } s} \left[\frac{l_s}{L} - \left(\frac{d_s}{2L} \right)^2 \right]$$

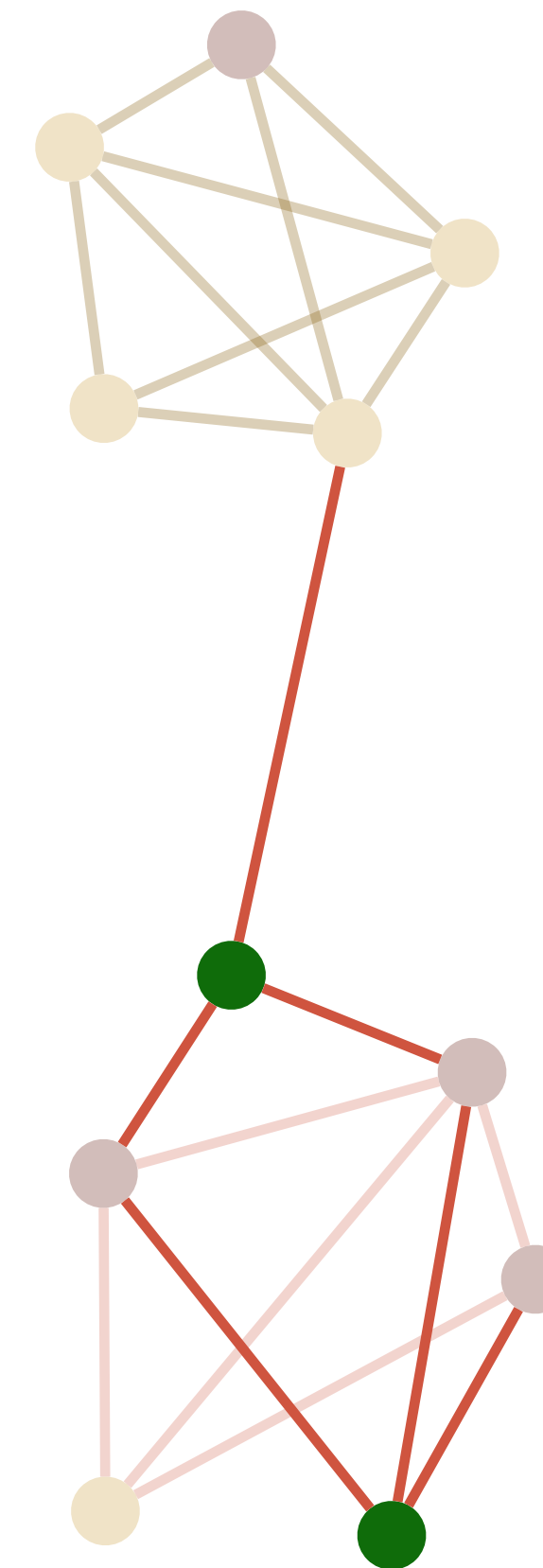


how to find the modules?

$$M = \sum_{\text{all modules } s} \left[\frac{l_s}{L} - \left(\frac{d_s}{2L} \right)^2 \right]$$



$$(0/20) - (6/40)^2$$



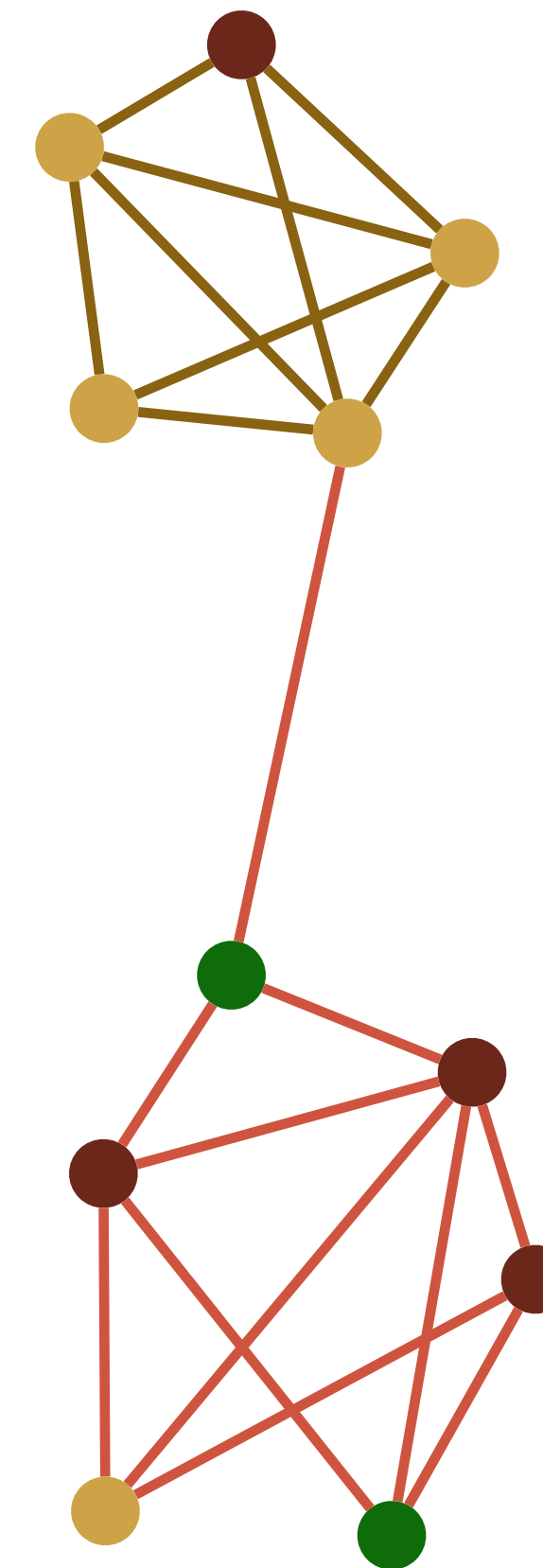
how to find the modules?

$$M = \sum_{\text{all modules } s} \left[\frac{l_s}{L} - \left(\frac{d_s}{2L} \right)^2 \right]$$

● $(2/20) - (15/40)^2$

● $(6/20) - (18/40)^2$

● $(0/20) - (6/40)^2$



how to find the modules?

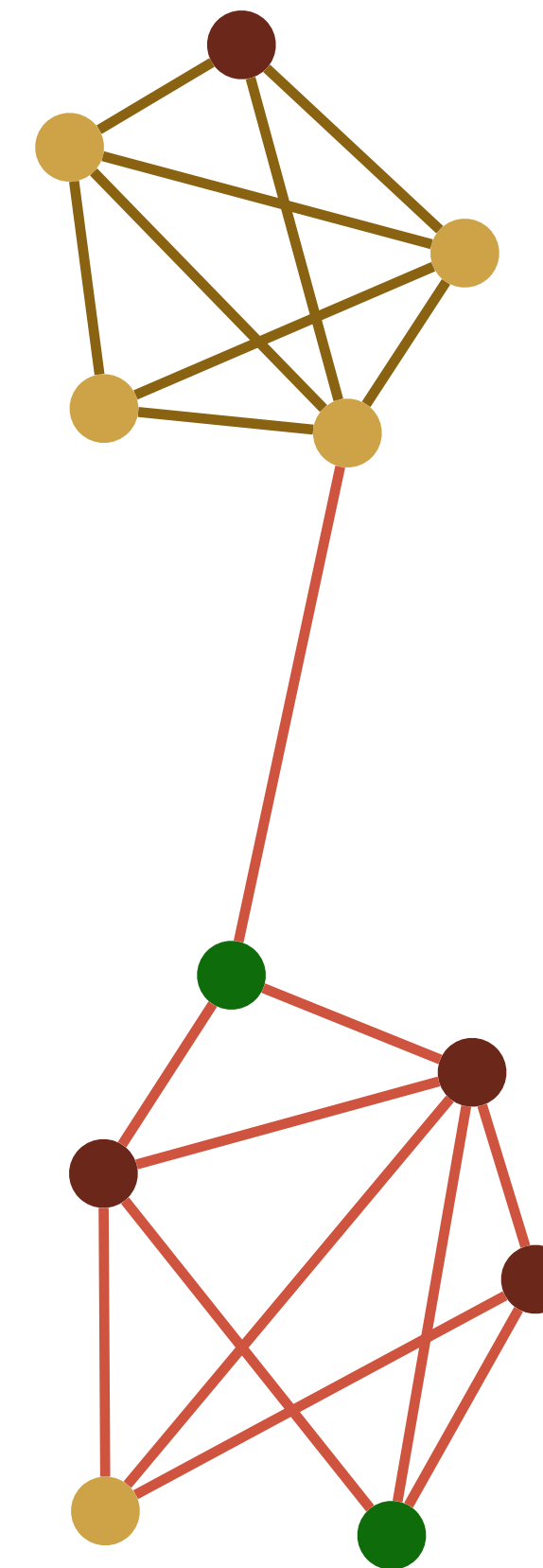
$$M = \sum_{\text{all modules } s} \left[\frac{l_s}{L} - \left(\frac{d_s}{2L} \right)^2 \right]$$

● - 0.04

● 0.10

● - 0.02

M = 0.04



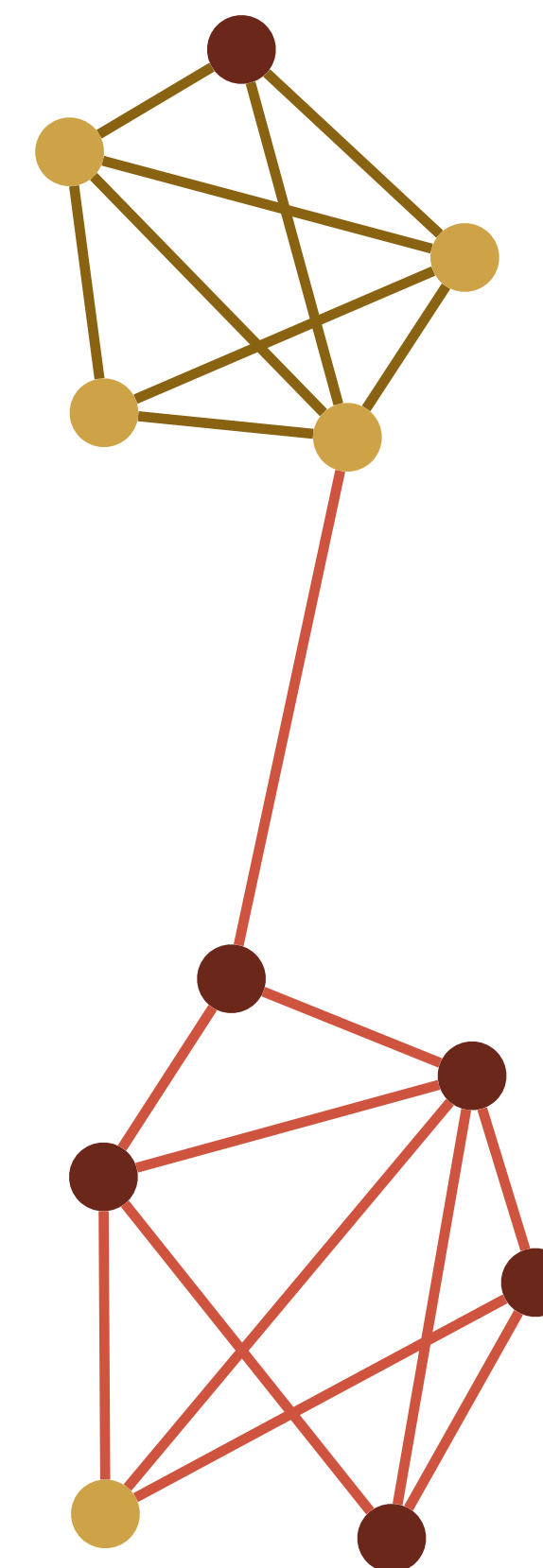
how to find the modules?

$$M = \sum_{\text{all modules } s} \left[\frac{l_s}{L} - \left(\frac{d_s}{2L} \right)^2 \right]$$

● 0.01

● 0.15

M = 0.16



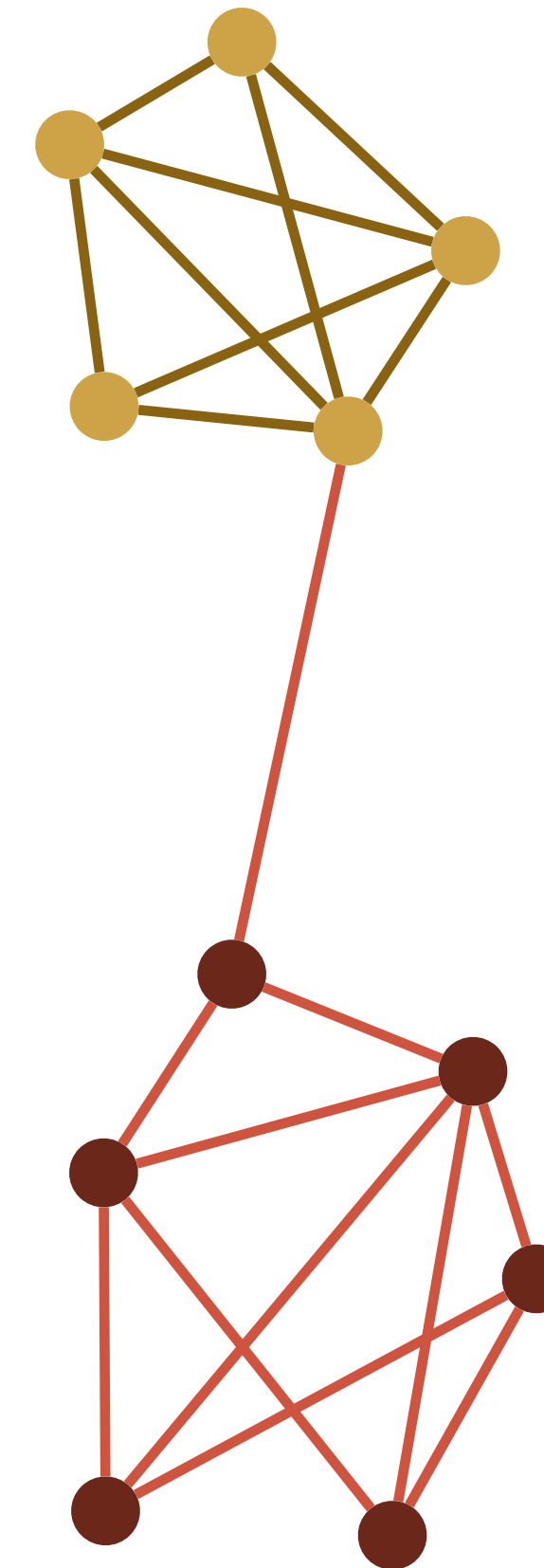
how to find the modules?

$$M = \sum_{\text{all modules } s} \left[\frac{l_s}{L} - \left(\frac{d_s}{2L} \right)^2 \right]$$

● 0.22

● 0.25

M = 0.47

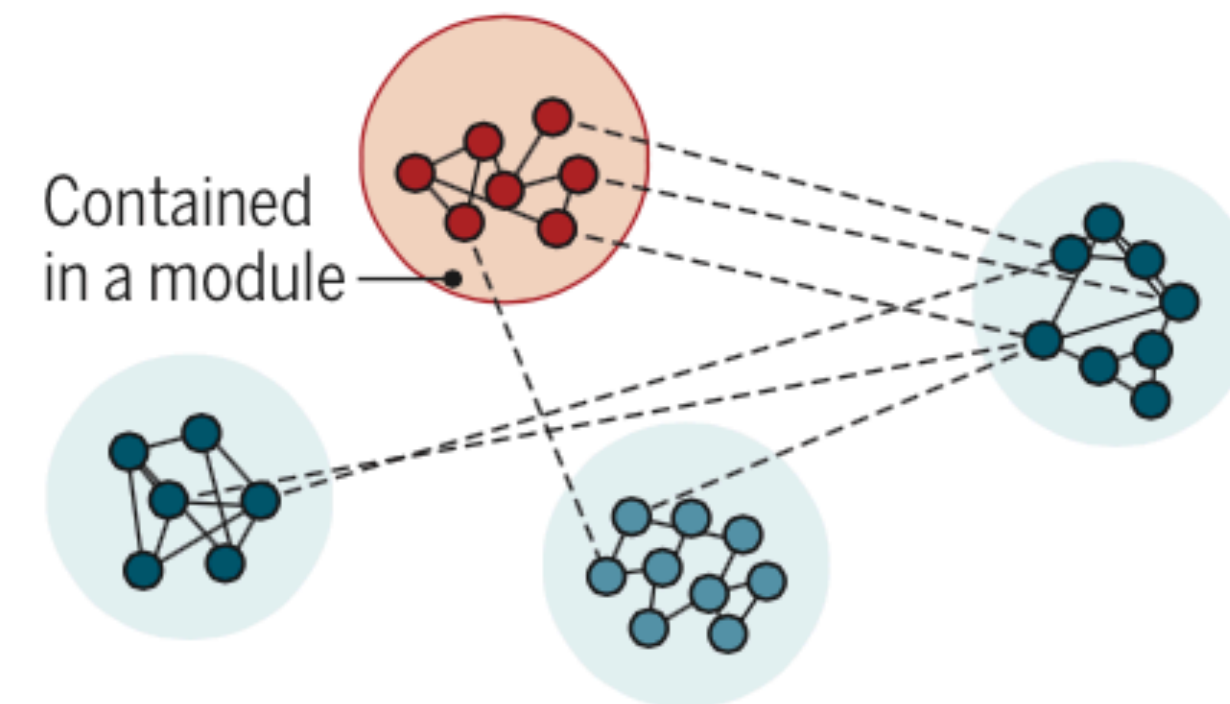
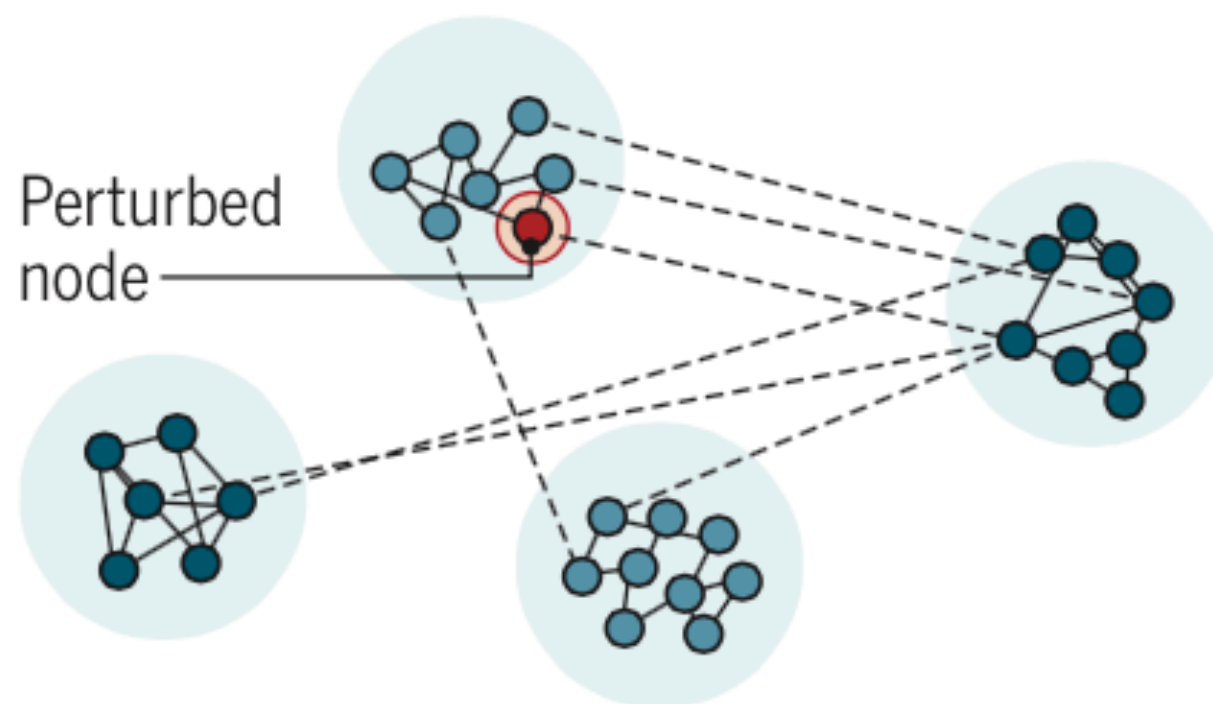
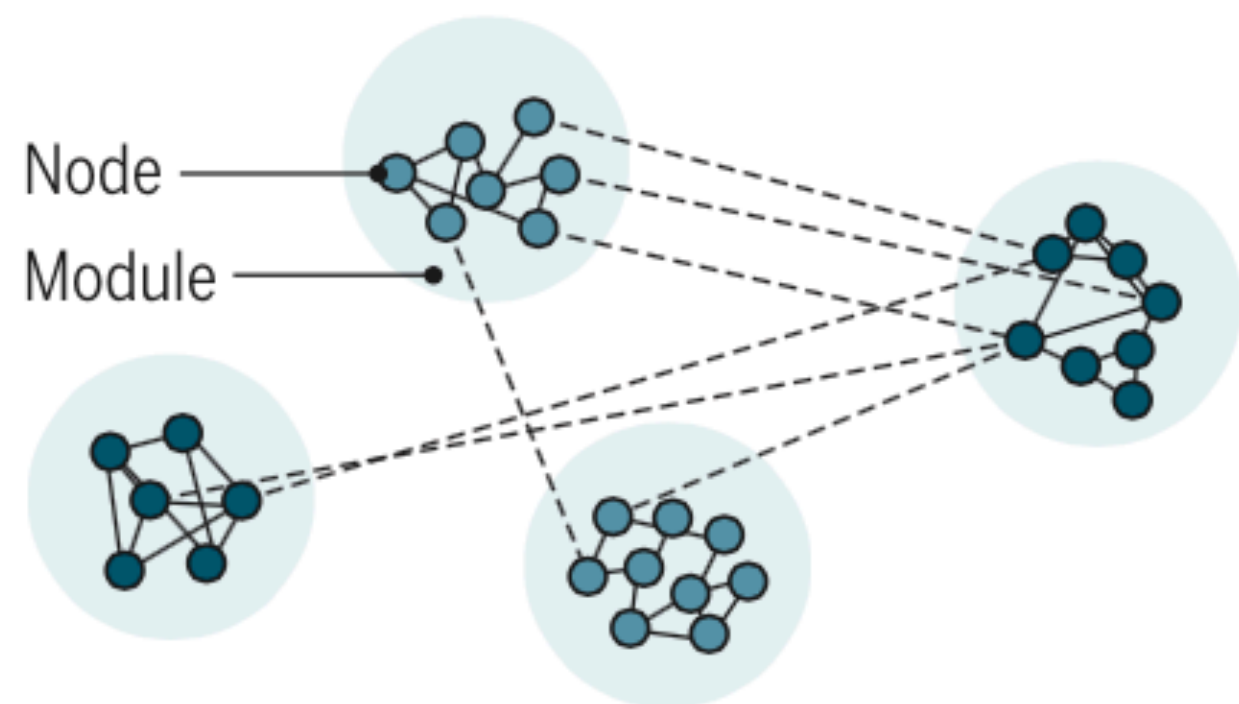


System state

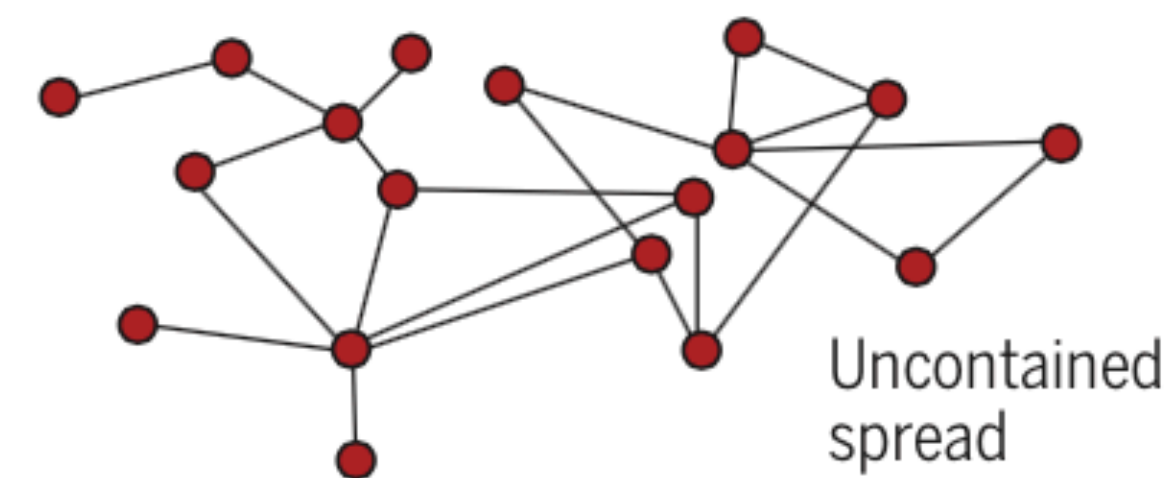
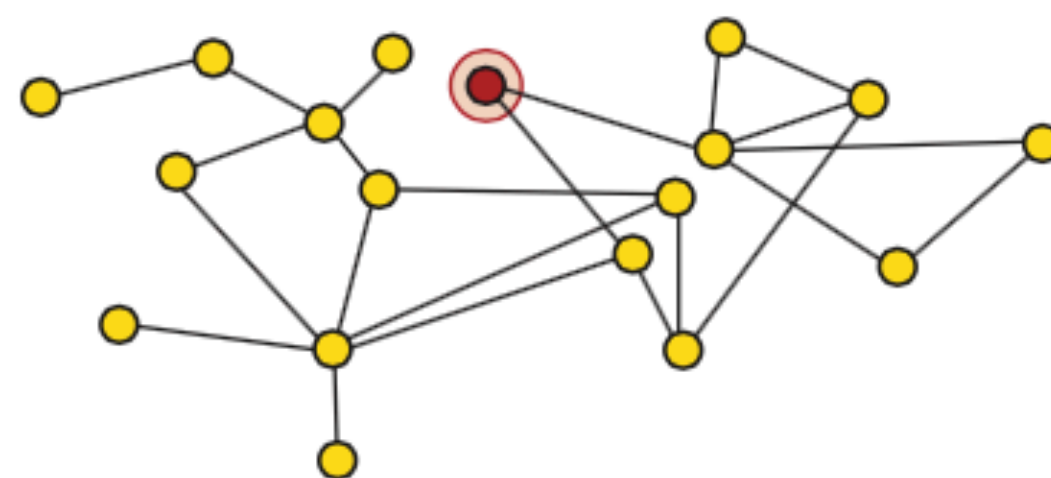
Perturbation starts

Perturbation spreads

Modular



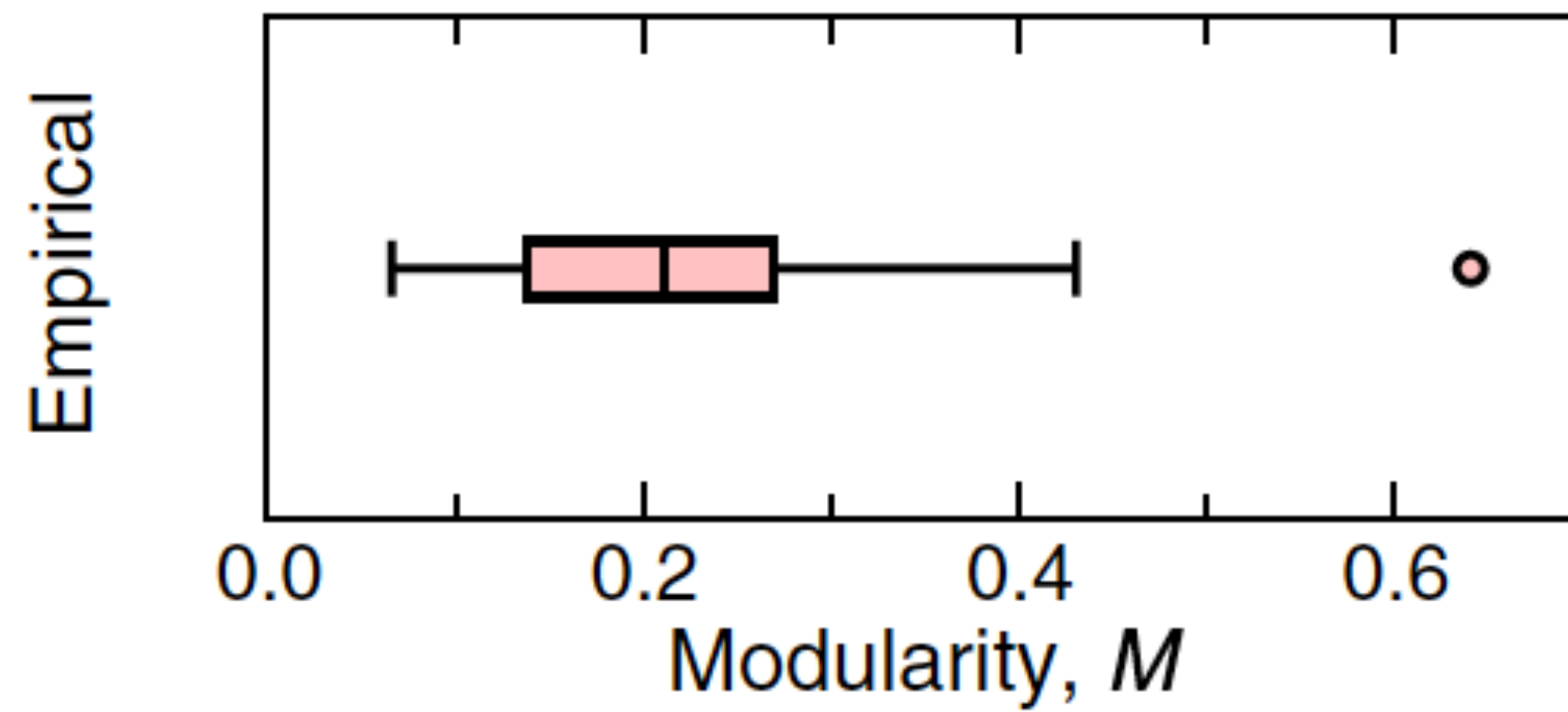
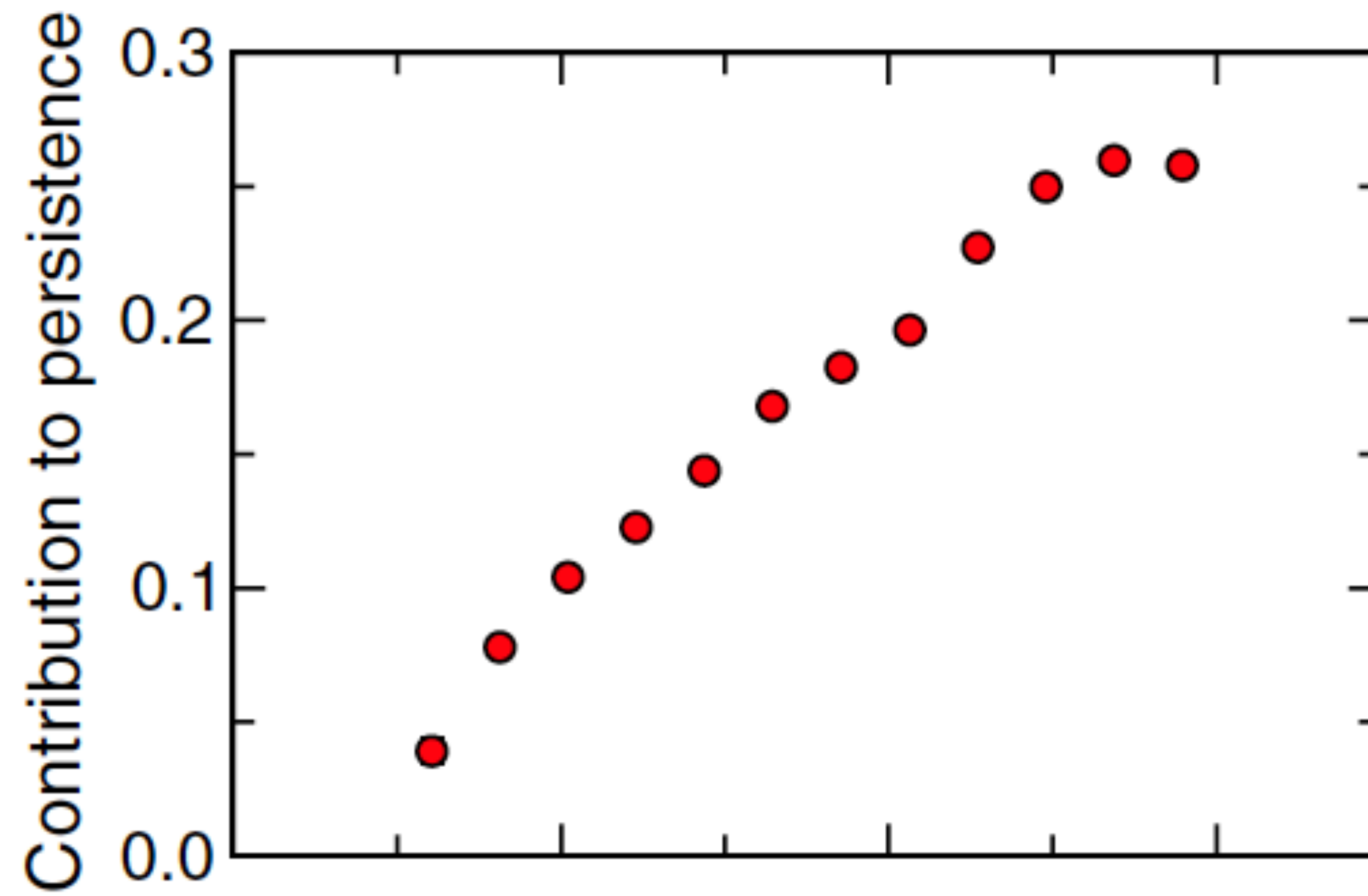
Random

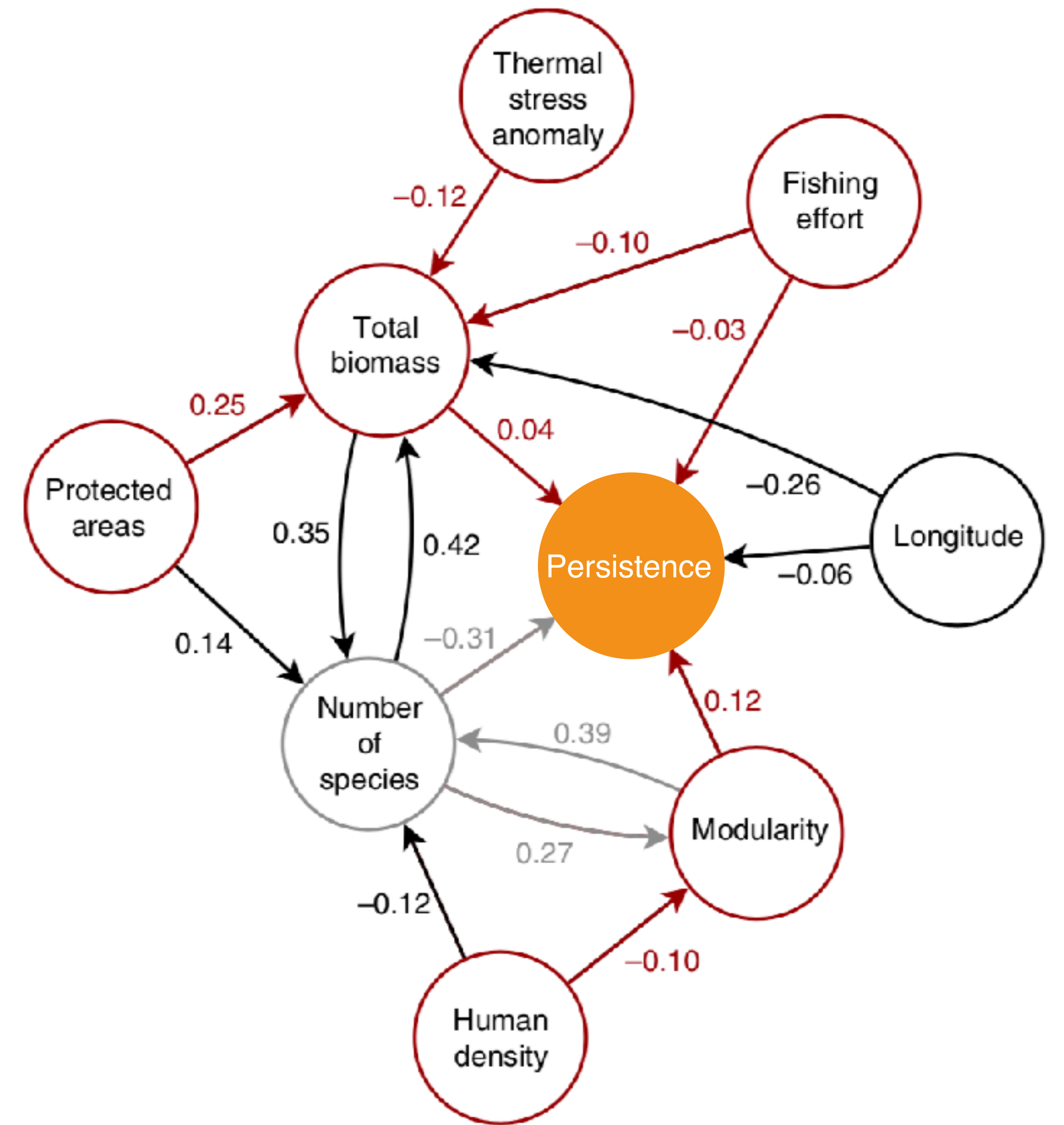
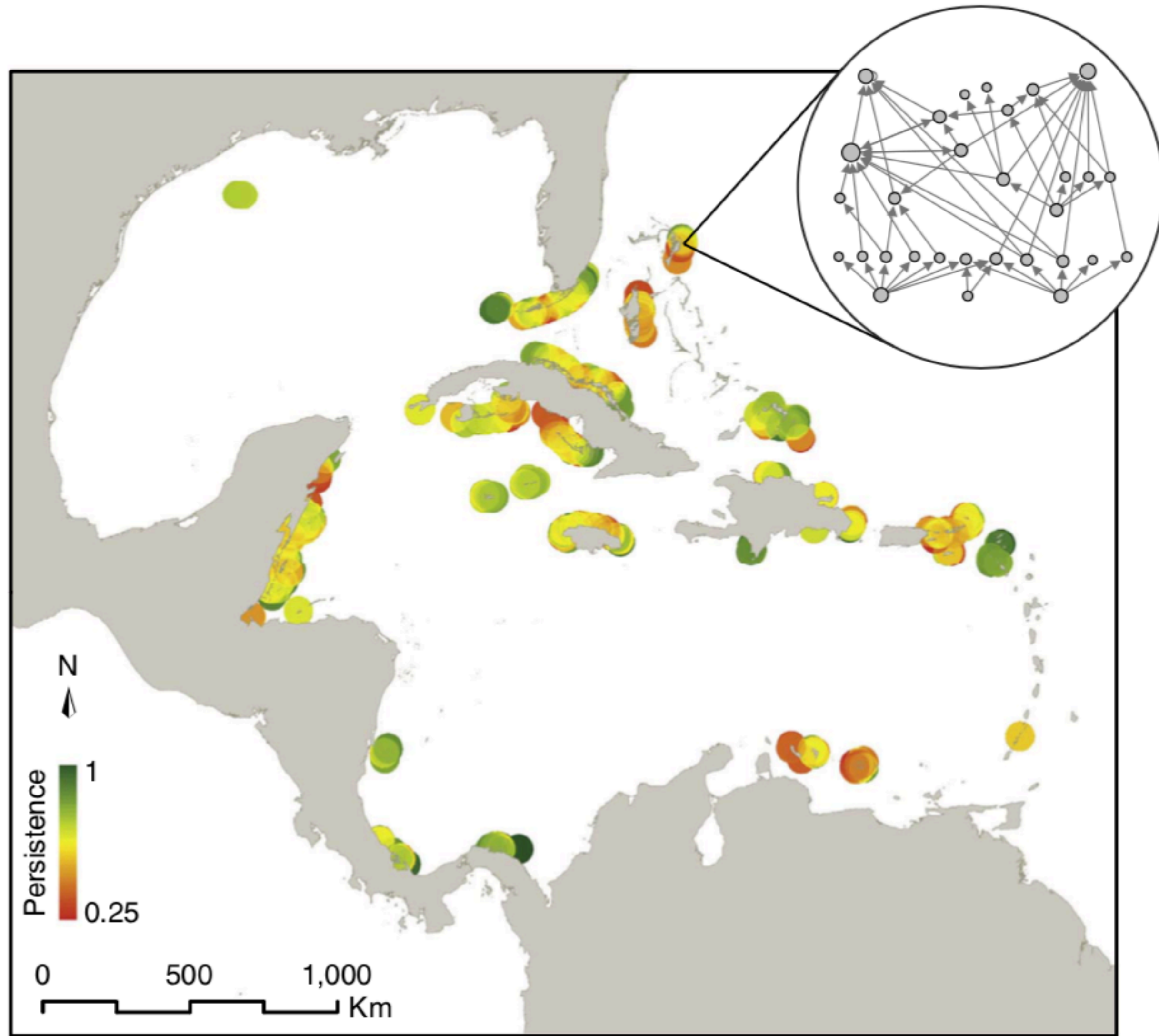


a metabolic model of a food web

$$\frac{dB_i}{dt} = r_i G_i B_i - B_i x_i + B_i x_i \sum_{j=prey}^n y_i F_{ij} - \sum_{k=pred}^n \frac{x_k y_k B_k F_{ki}}{e_{ki}}$$

(The change in biomass is a function of growth, respiration, and biomass gain and loss through predation)





[Gilarranz, Mora, and Bascompte (2016) *Nat. Commun.* 7: 10737]