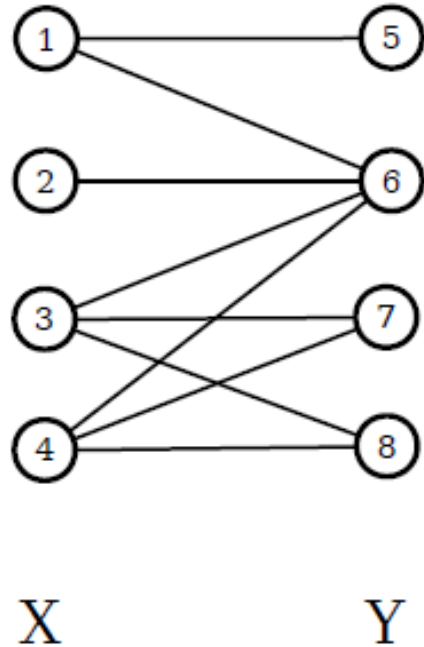


Measuring Connectance and Nestedness

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Bipartite networks



n_x - number of nodes in set X (rows)

n_y - number of nodes in set Y (columns)

m - number of links in the network

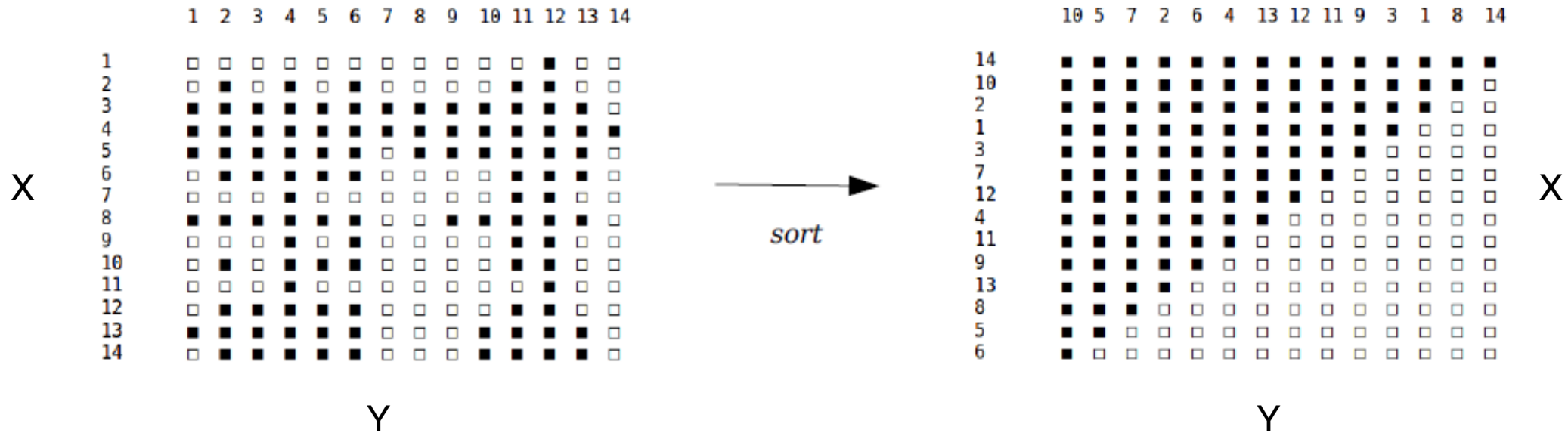
Connectance C of a bipartite network is given by:

$$C = \frac{m}{n_x n_y}$$

Two sets (groups) of nodes (X and Y).
There are only connections between nodes that do not belong to the same set.

Nestedness

Sort columns and rows of the incidence matrix by the degrees of the nodes:



A network is nested, if for both groups X and Y :

- 1) there are nodes with many interactions (generalists) and nodes with a few interactions (specialists)
- 2) the nodes with few interactions share the interactions with the nodes with many interactions

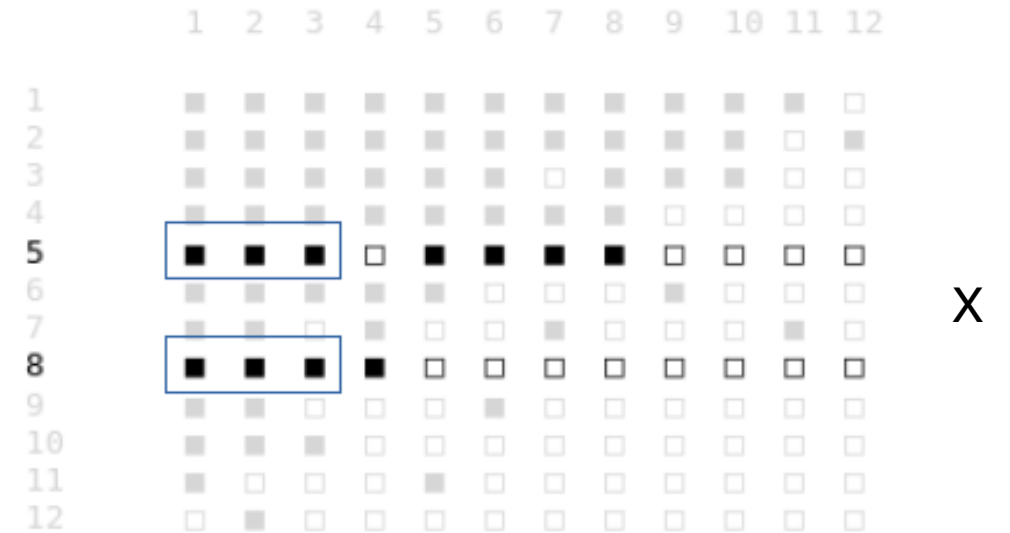
Calculating nestedness – Fortuna et al. (2019)

The overlap o_{ij} between two nodes i and j (from the same group) is the fraction of interactions of the node with the smaller degree that are shared by the node with the larger degree.

$$o_{ij} = \frac{c_{ij}}{\min(k_i, k_j)}$$

c_{ij} - the number of interactions node i and j share

$$c_{ij} = \sum_{k=1}^{n_y} B_{i,k} B_{j,k} \quad (\text{for rows})$$



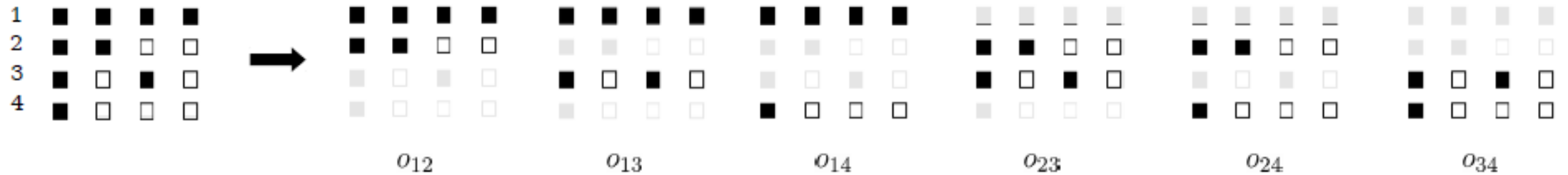
Example: overlap between node 5 and node 8 is:

$$o_{5,8} = \frac{3}{\min(7,4)} = \frac{3}{4}$$

Calculating nestedness – Fortuna et al. (2019)

Step 1: calculate the overlap of all pairs of rows

$$\sum_{i=1, i < j}^{n_x} o_{ij}$$



Step 2: calculate the overlap of all pairs of columns

$$\sum_{i=1, i < j}^{n_y} o_{ij}$$

Calculating nestedness – Fortuna et al. (2019)

Step 3: calculate nestedness N of the network – the average overlap of all pairs of rows and all pairs of columns:

$$N = \frac{\sum_{i=1, i < j}^{n_x} o_{ij} + \sum_{i=1, i < j}^{n_y} o_{ij}}{\frac{n_x(n_x - 1)}{2} + \frac{n_y(n_y - 1)}{2}}$$

N has values between 0 (not nested) and 1 (perfectly nested).